AL FURAT AL AWSAT TECHNICAL UNIVERSITY NAJAF COLLEGE OF TECHNOLOGY DEPARTMENT OF AVIONICS ENGINEERING

DIGITAL SIGNAL PROCESSING

3rd YEAR

BY
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Discrete Correlation

- Correlation or "Co-Relation" is a measure of similarity/ relationship between two signals.
- If x[n] & y[n] are two discrete-time signals, then the correlation of x[n] with respect to y[n] is given as,

$$r_{xy}[l] = \sum_{m=-\infty}^{\infty} x[m] \ y[m-l]$$

where L is lag, indicating time-shift.

Relationship b/w Conv. & Corr.

Mathematically, Convolution between x[n] & h[n] is given as:

$$y[n] = \sum_{k=-\infty}^{\infty} x[k] \ h[n-k]$$

Correlation of x[n] with h[n] is given as:

$$r[n] = \sum_{k=-\infty}^{\infty} x[k] \ h[k-n]$$

Relationship b/w Conv. & Corr.

But if we "time-reversed" the second sequence of the Convolution, we end up with Correlation

$$y[n] = \sum_{k=-\infty}^{\infty} x[k] \ h[-(n-k)]$$
$$= \sum_{k=-\infty}^{\infty} x[k] \ h[-n+k]$$
$$r[n] = \sum_{k=-\infty}^{\infty} x[k] \ h[k-n]$$

Where, r[n] is the correlation of x[n] with respect to h[n].

Relationship b/w Conv. & Corr.

➤ So, we can say that "Correlation, mathematically, is just Convolution, with the second sequence, time-reversed"

$$r[n] = x[n] * h[-n]$$

- ▶ We can use this property to find Correlation, using the same method we used for Convolution, albeit, the second sequence needs to be time-reversed.
- ▶ This only requires that we don't time-reverse for convolution in the first place!

notes for solving the correlation's problems

length of 1st sequence = Li

length of 2nd sequence = Lz

length of output sequence = Litz-1

notes for solving the correlation's problems

First sequence start at n=n1

se cond sequence start at n=n2

output sequence Start at ni-(n2+L2-1)

output sequence ends at SP+(LI+LZ-2)

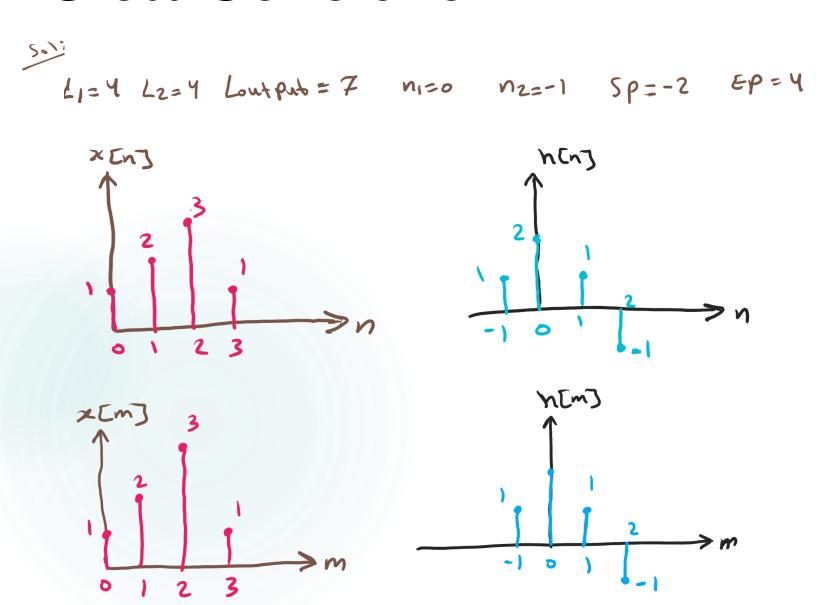
Types of discrete correlation

- ▶ There are two types of correlation:
- 1. Cross correlation:

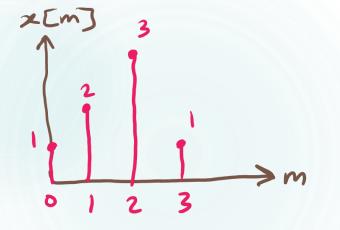
It is a comparison of two different signals.

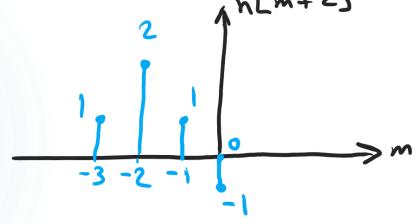
2. Auto correlation:

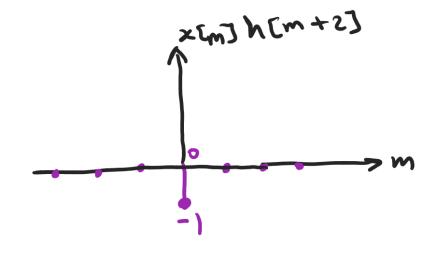
It is a comparison of the signal with itself at a different time.

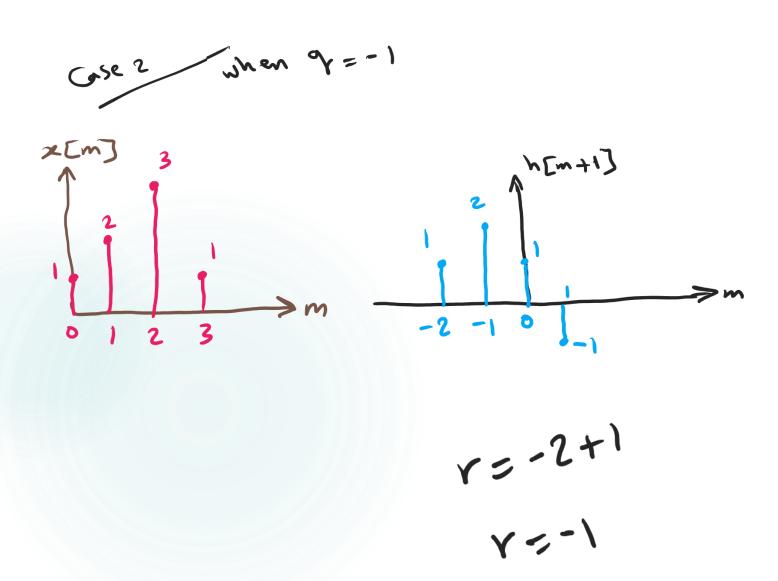


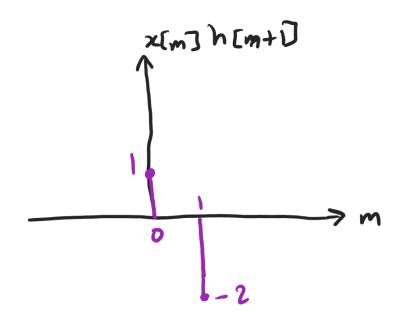


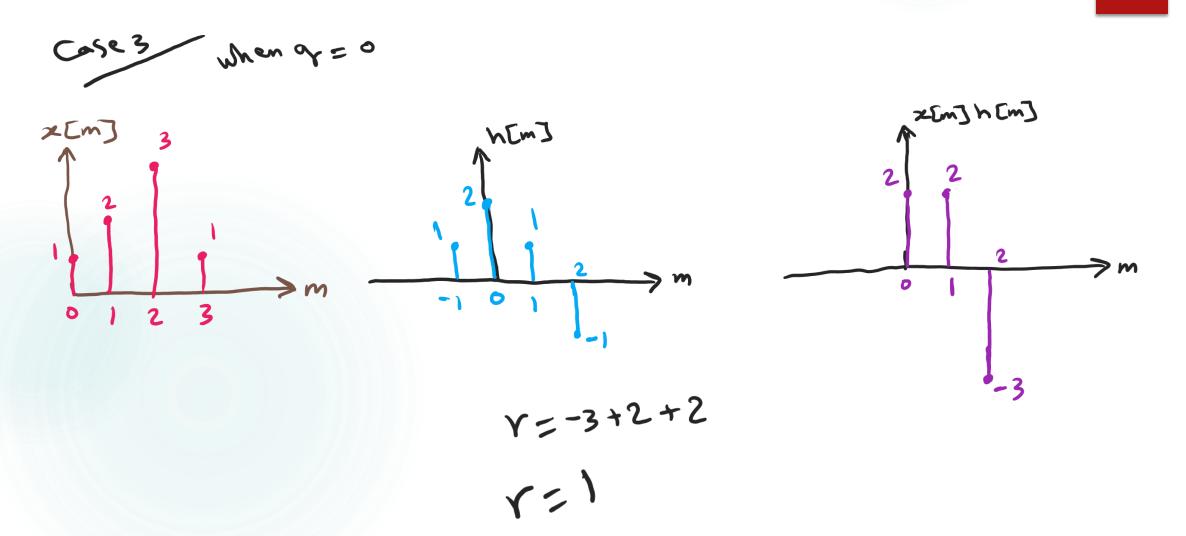


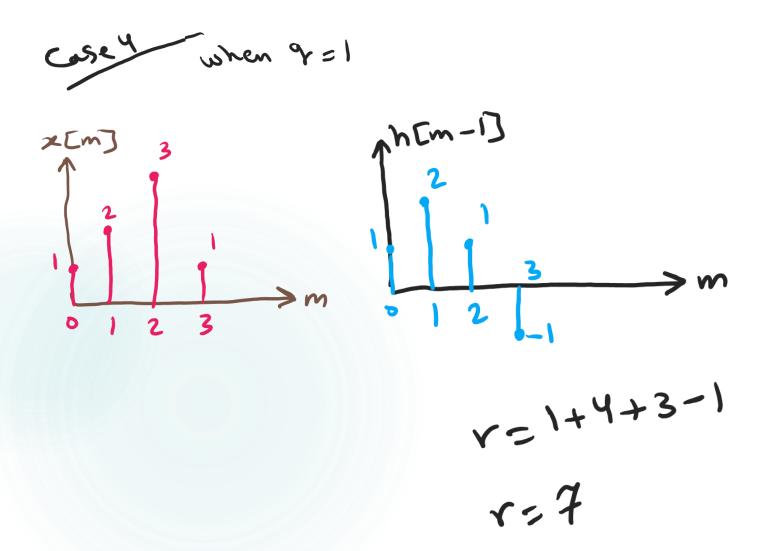






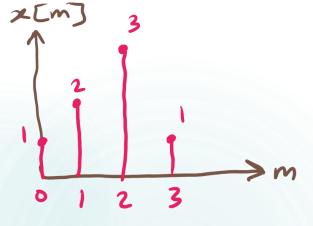


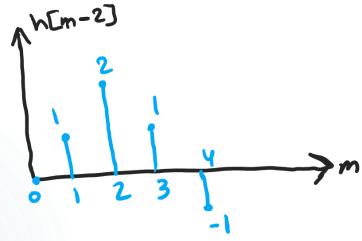


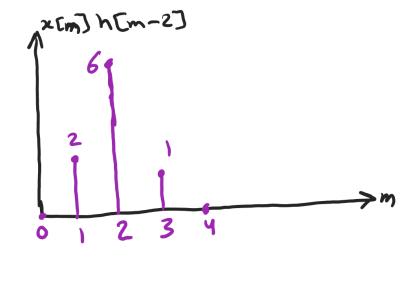


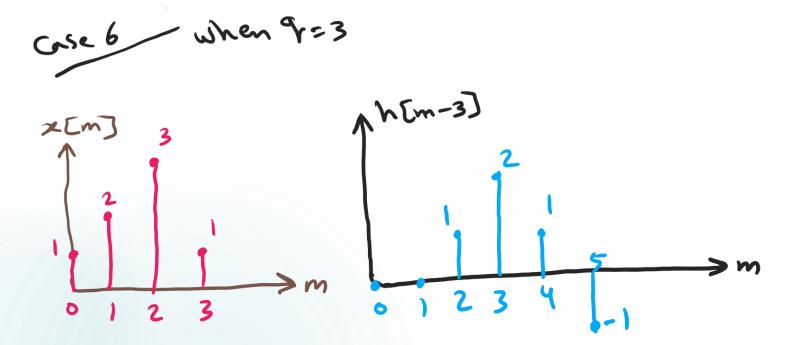


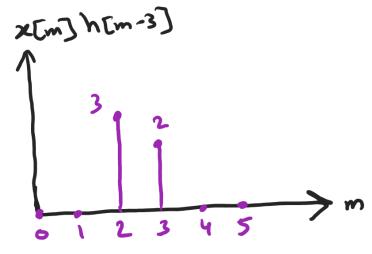


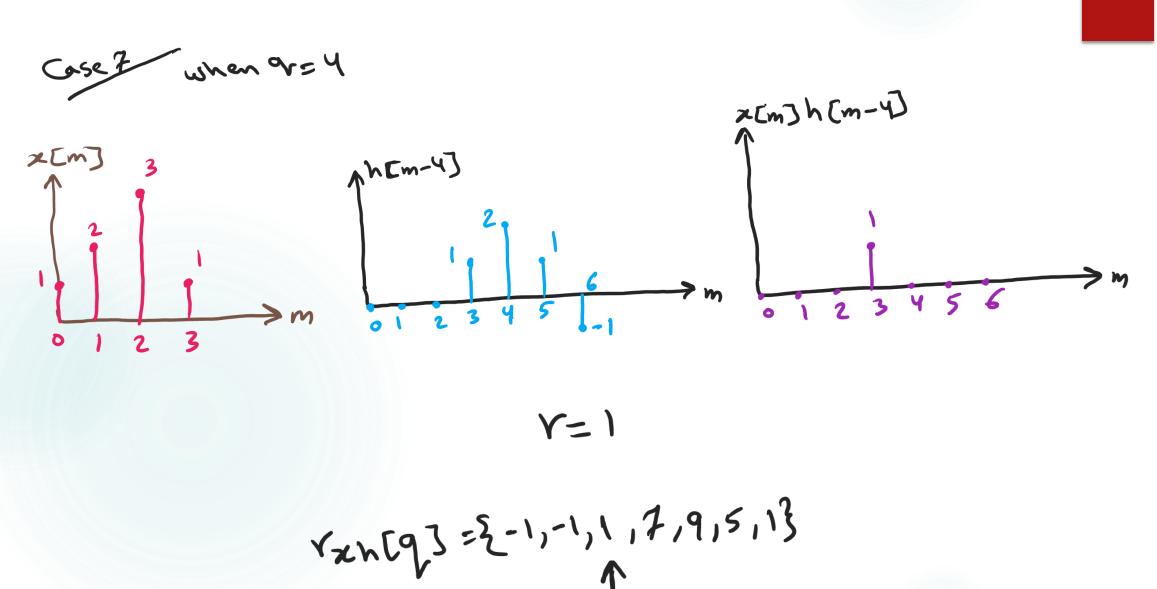


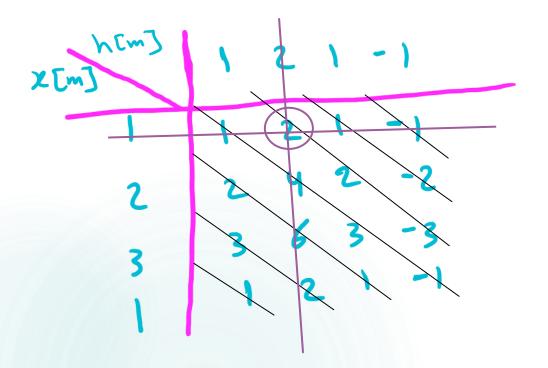








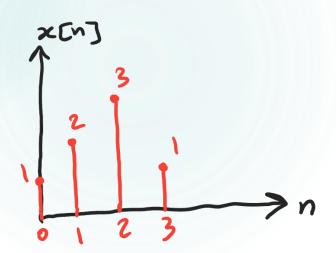


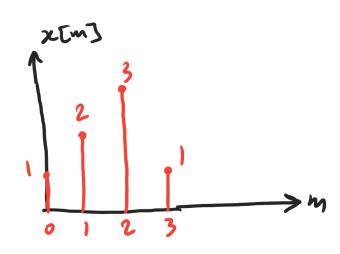


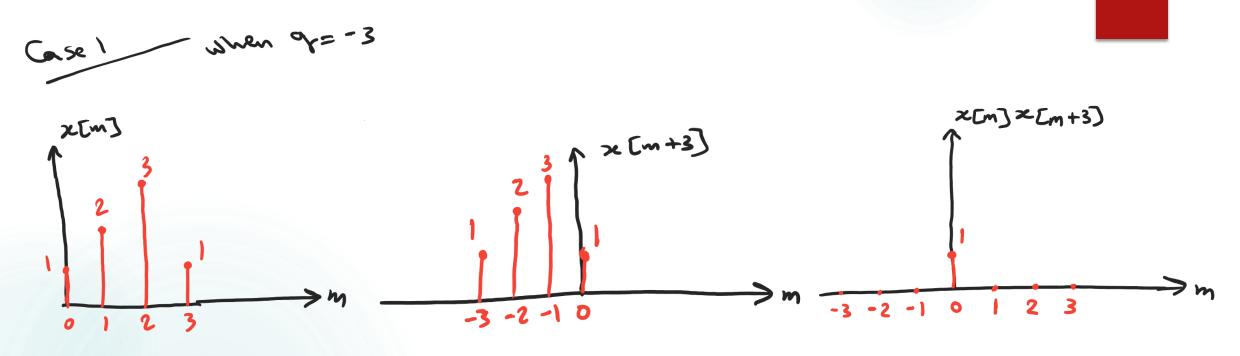
Ex/ Find the auto Greelation of the following sequence

x(n) = 2/12,3,13

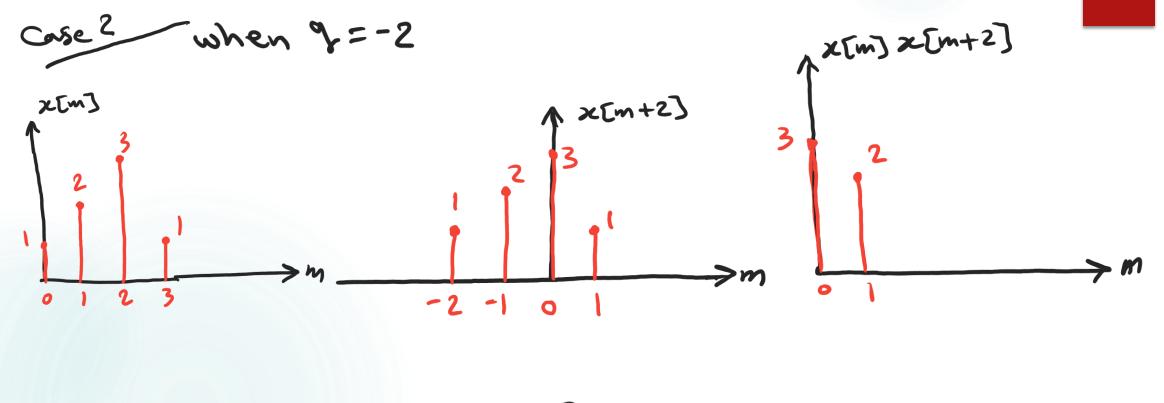
length of o/p=7 n1=n2=0 SP=-3 EP=



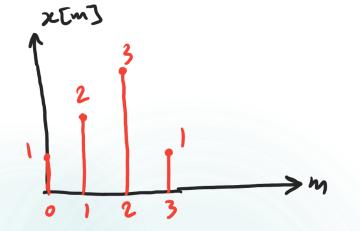


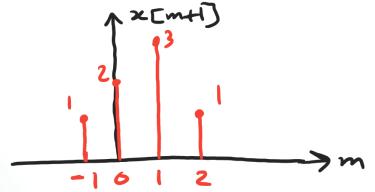






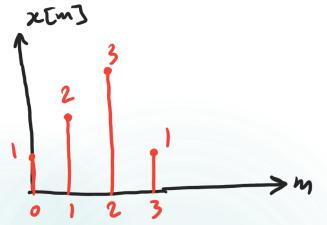


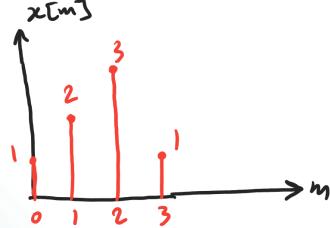




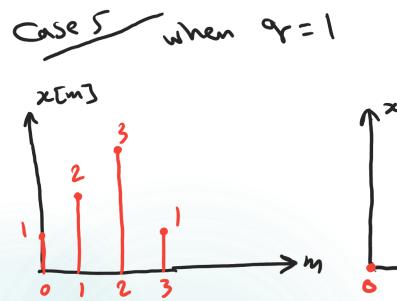


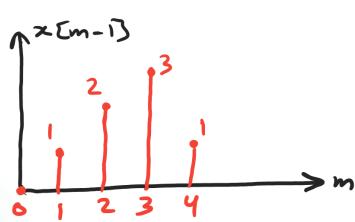


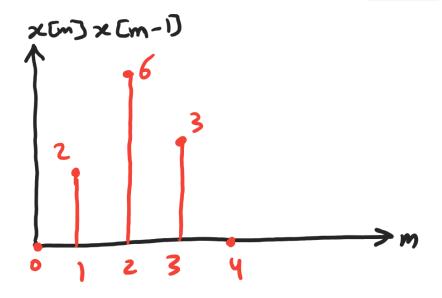












$$V = 2 + 6 + 3$$
 $V = 11$



